

# Ασκήσεις

ma12715

## Άσκηση 1 - Διαφορικές εξισώσεις

$$\mu(x) = e^{\int \tan x dx} = \frac{1}{\cos x}$$

Πολλαπλασιάζουμε:

$$\begin{aligned} \frac{x}{dx} \left( \frac{y}{\cos x} \right) &= \tan x \Rightarrow \frac{y}{\cos x} = \int \tan x dx = -\ln |\cos x| + c \\ \frac{x^2}{(x+1)^3} &= \frac{A}{x+1} + \dots + \frac{C}{(x+1)^3} \end{aligned} \tag{1}$$

Με βάση την εξίσωση 1.

$$\begin{cases} A = 1 \\ 2A + B = 0 \Rightarrow B = -2 \\ A + B + C = 0 \Rightarrow 1 - 2 + C = 0 \Rightarrow C = 1 \end{cases} \tag{2}$$

$$\begin{aligned} A(x+1)^2 &= a(x^2 + 2x + 1) = Ax^2 + 2Ax + A \\ B(X+1) &= BX + B \\ \Rightarrow x^2 &= Ax^2 + (2A+B)x + (A+B+C) \end{aligned} \tag{3}$$

$$\lim_{x \rightarrow 0} \frac{e^x - \cos x - x \sin x - 1}{x^4} \int_{a=1}^n$$